

Grade

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## Published by

Asia-Pacific Centre of Education for International Understanding and
Philippine Normal University Manila, Philippines

Learning Area: Mathematics
Grade Level: 10
Title: Arithmetic Sequence and Its Application Project: Global Citizenship Education Curriculum Development and Integration in the Philippines

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ISBN: 979-11-87819-71-4
APCEIU Publication Number: BE-RND-2021-074

## Learning Area: Mathematics

## Grade Level: 10

Quarter: 1st
GCED Domain/s: Cognitive, Socio-Emotional and Behavioral

## GCED Indicator/s:

D.1.1.a. Recognize complex situations or problems
D.1.1.e Evaluate appropriate actions, consequences, and implications
D.2.1.e Commit to assume responsibility, mutual assistance, cooperation, and collaboration in various contexts in the world.
D.3.1.b. Initiate actions about local, national or global issues

## GCED Topic/s:

T1.3. Interconnectedness of global, national and local systems

## Enhanced Content Standard/s:

Demonstrates understanding of key concepts of sequences, polynomials and polynomial equations relevant to local, national, or global community.

## Enhanced Performance Standard/s:

Is able to formulate and solve local, national, or global problems on climate change involving sequences, polynomials and polynomial equations in different disciplines through appropriate and accurate representations.

## Time Allotment:

60-90 minutes

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## ARITHMETHIC SEQUENCE AND ITS APPLICATION



## LESSON INTRODUCTION

The earth is in danger, and everyone faces our greatest fear, the consequences of climate change. Floods, disease, and famine have led to unprecedented large-scale migration in already highly stressed areas; droughts and crop failures have led to increased competition for food, and water; wildlife is put to higher risks where animal and plant species are struggling to cope. Climate change affects all regions of the world and its impacts are to surge in the years to come.

To learn more about climate change particularly global warming, its causes and consequences, watch the video by following the link: https://www.youtube.com/ watch? $v=d c B X m j 7 n M T Q$.

The documentary featured facts demonstrating that carbon dioxide is one of the most destructive greenhouse gases in the atmosphere, continuously raising the earth's temperature and causing global warming. Many experts believe that rising temperatures is caused by increased carbon dioxide levels in the atmosphere. The combustion of fossil fuels produces carbon dioxide as a byproduct.

World Trade Organization (WTO, 2010) reported, "The lack of business responsibility has led to growth without conscience: an unsustainable growth that is oblivious to what we have done to the environment and an excessive consumption culture disregarding its impact on future generations. The planet Earth can sustainably support a maximum of 430 to 450 parts per million (ppm) of CO2 in a given volume of air. We are already at 390 ppm and increasing at the rate of 2 ppm per year. If we do nothing, we will face a catastrophic calamity - which is only 20 to 30 years away - that will not distinguish between rich or poor, north or south, race or religion."

For you to gain a better picture and understanding of the impact of the Earth's CO2 profile on the climate crisis the world is experiencing today, the reported data can be translated and illustrated into an ARITHMETIC SEQUENCE.

This material provides you with activities that will help you learn all about arithmetic sequence. More than that, activities in this module will create awareness of the contributing factors of climate change, one of the most important issues our world is facing today.

## LISSON OBJECTIVE

## A. Cognitive

1.Recognize the problems and issues on climate change specifically on carbon dioxide emission;
2. Evaluate appropriate actions, consequences and implications of carbon dioxide composition;
3.Find the nthterm of an arithmetic sequence;
4.Illustrate arithmetic sequence depicted in carbon dioxide emission in the atmosphere ;
5.Formulate equation of arithmetic sequence on word problems related to climate change.

## B. Socio-Emotional

6. Appreciate the use of arithmetic sequences in discoursing and addressing climate change issues on carbon dioxide emission;
7. Commit to assume responsibility, mutual assistance, cooperation, and collaboration in addressing climate change.

## C. Behavioral

8.Take individual action to help address climate change by initiating carbon dioxide offsetting measures at household or community level.

## PRETEST <br> (WHAT I NEED TO KNOW / SUBUKIN)

How well do you understand arithmetic sequences and their applications?

## Part A

Directions: Choose the letter that corresponds to the answer of each item. Write your answer in a separate answer sheet.

1. What is the common difference in the arithmetic sequence $2,7,12,17, \ldots$ ?
a. 2
B. 5
C. 17
D. 20
2. What is the 100thterm of the sequence of the given the sequence $-10,-5,0,5, \ldots$ ?
a. 500
B. 485
C. 1005
D. 355
3. Which among the given situations DOES NOT illustrate an arithmetic sequence?
a. Between 2009-2018, the growth rate of CO2 emission has been 2.3 ppm per year.
b. There are numerous methods for increasing carbon in soils. Planting cover crops in fields that would otherwise be bare can extend photosynthesis throughout the year, sequestering approximately half a metric ton of CO2 per acre per year.
c. The potential for carbon removal from the forests and trees outside of forests in the United States alone is more than a half gigatonne per year.
d. The number of cases in the Philippines can be modelled by the equation an = 1 OOO (1.61n-1), where an is the number of COVID-19 infections after $n$ months.
4. According to the most recent United Nations estimates elaborated by Worldometer, the current world population is 7.9 billion as of June 2021. What is the equation for calculating the projected population after $n$ years if global human population growth is 75 million per year?
a. $a n=1000(7.9 n-1)$
b. $a n=7.9(n-7) 75000000$
c. $a n=7900000000+(n-1) 75000000$
d. $a n=75000000+(n-7) 7.9$

Direction: Answer the question.
How can understanding of arithmetic sequences help you to make an informed decision on mitigating the causes and consequences of climate change?

## LESSON PROPER

## REVIEW (WHAT'S IN/BALIKAN)

Before we get into the arithmetic sequence, we will test your knowledge of patterns and sequences.

A pattern in mathematics is a repeated arrangement of numbers, shapes, and colors and so on. The Pattern can be associated with any kind of event or object. Patterns can have a finite or infinite number of variations. A sequence is a set or chain of numbers that usually follows a particular pattern.

The scenarios and problems presented below address the activity's goal (PATTERNS and SEQUENCES).

Directions: Each item below shows a pattern. Write your answer in a separate sheet of paper.

1. A greenhouse gas (GHG or GhG) is a gas that absorbs and emits radiant energy due to the gravitational pull of the Earth. These gases are methane ( CH 4 ), nitrous oxide ( N 2 O ), argon ( Ar ) , carbon dioxide (CO2 ), and ozone (O3). What are the next three symbols in the following sequence?
$\mathrm{CH} 4, \mathrm{~N} 2 \mathrm{O}, \mathrm{Ar}, \mathrm{CO} 2, \mathrm{O} 3, \mathrm{CH} 4, \mathrm{CH} 4, \mathrm{~N} 2 \mathrm{O}, \mathrm{N} 2 \mathrm{O}, \mathrm{Ar}, \mathrm{Ar}, \mathrm{CO} 2, \mathrm{CO} 2, \mathrm{O} 3, \mathrm{O} 3, \mathrm{CH} 4, \mathrm{CH} 4, \ldots$
A. $\mathrm{N} 2 \mathrm{O}, \mathrm{N} 2 \mathrm{O}, \mathrm{N} 2 \mathrm{O}$,
B. $\mathrm{CH} 4, \mathrm{~N} 2 \mathrm{O}, \mathrm{Ar}$
C. , Ar, Ar, CO2
D. $\mathrm{CH} 4, \mathrm{~N} 2 \mathrm{O}, \mathrm{N} 2 \mathrm{O}$
2. What is the next number in the sequence $0,6,12,18,24, \ldots$ ?
A. 30
B. 36
C. 42
D. 48

## LESSON PROPAR

## ACTIVITY (WHAT'S NEW/TUKLASIN)

## Activity 1: Watch and Learn!

## Directions:

Watch the video by following the link (32) WeatherMinds: New study shows carbon dioxide levels increasing - YouTube.

Take note of important details.

Answer the following questions to ponder.

1. What facts or important data related to climate change and global warming were discussed in the video?
2. Are these facts new to you? If not, when and from whom did you learn them?

## Activity 2: Carbon Arithmetic

Directions:
Read the report given by World Trade Organization in one of their discussions during the public forum held in 2009 and answer the guide questions that follow to complete the table of values

According to reports, the earth's carbon dioxide abundance is already at 390 ppm in a given volume of air in 2009 and is steadily increasing at a rate of 2ppm per year.

| Year | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 |
| :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| $\mathrm{CO}_{2}$ in ppm | 390 | $?$ | $?$ | $?$ | $?$ | $?$ |

## LESSON PROPER

## ACTIVITY (WHAT'S NEW/TUKLASIN)

Guide Questions:

1. Given that CO2 are rising by 2ppm per year, what is the expected CO2 per volume in 2010? What about 2011? What method did you use to solve it?
2. How much CO2 was produced in 2014? What about in 2021?
3. How many parts per million (ppm) of CO2 will be there in 100 years from year 2009?
4. How did you calculate the expected volume of CO 2 in the previous question?

We can calculate the volume of CO2 in parts per million after a few years for you. Use the concepts of arithmetic sequence or arithmetic progression to solve it.

## LESSON PROPER

## DISCUSSION (WHAT IS IT/TALAKAYIN)

An arithmetic sequence, also known as arithmetic progression, is a sequence of numbers where the next term is obtained by getting the sum of the term and the common difference. The common difference of an arithmetic sequence is the difference of a term and the term immediately before it in the sequence.

## Example A

Based on the previous activity, the CO2 sequence in ppm is 390, 392, 394, 396, 398, $400,402,404$ which is an arithmetic sequence with a common difference of 2 .

The nth term (an) of an arithmetic sequence with a common difference(d) can be computed by
an =al + (n-1)d.

For this example, we have al= 390, a2= 392, a3=394, a4=396, a5=398, a6=400, and so on.

1. CO2 abundance in 2009 is 390 ppm, how abundant is CO 2 in 2019 using the increasing rate of $2 p p m$ ?

Solve: an =al + $\mathrm{n}-1$ ) d
Using the given, $\mathrm{al}=390$ and $\mathrm{d}=2$. Determine the value of n using the formula.

Since al starts at year 2009, and we are to solve for the year 2019, $n$ is the number of years from 2009 to 2019. Hence $n=11$. Use the formula for an.

$$
\begin{gathered}
\text { a11 }=390+(11-1) 2 \text { a11 }=392+(10) 2 \\
\text { al1 }=392+20 \\
\text { a11 }=412
\end{gathered}
$$

## LESSON PROPER

## DISCUSSION (WHAT IS IT/TALAKAYIN)

Using the same situation in the previous item, what is a50 ?
Solve: $a n=a 1+(n-1) d$
a50 $=390+(50-7) 2$
$a 50=390+(49) 2$
$a 50=390+98$
$a 50=488$

Guide Questions:

1. Given that the planet Earth can sustainably support a maximum of 430 to 450 ppm of CO 2 in the atmosphere and based on your computed value for the 50th year beginning in 2009, what can you say about the difference of the computed value and the maximum parts per million of CO2 that Earth could support?
2. What can you do to minimize the increase of CO ?

## Example B

Find the 16th term of the arithmetic sequence 12, 18, 24, 30, 36, ...

Solution:
Given: $a 7=13, d=31-25=6, n=16$ and use the equation $a n=a 1+(n-7) d$

$$
\begin{gathered}
\mathrm{a} 16=13+(16-7) 6=13+15(6) \\
=103
\end{gathered}
$$

The 16thterm of the sequence is 103 .

## LASSON PROPER

## GENERALIZATION (WHAT I HAVE LEARNED/ISAISIP)

A. Answer the following to summarize what you have learned from this module.

1. How has the concept of arithmetic sequence helped you in comprehending the trend of carbon dioxide abundance in the coming years?
2. What can each individual do to help reduce CO2 emissions?
3. How significant is the understanding of arithmetic sequence in solving real-world problems on climate change?
4. Provide an example of real-world problem that can be modeled by arithmetic sequence.

## LESSON PROPER

## REFLECTION (WHY IS IT MEANINGFUL AND RELEVANT/ISAPUSO)

Directions: Based on the graph and data provided, answer the guide questions that follow.


Source: Global Carbon Project; Carbon Dioxide Information Analysis Centre (CDIAC)
Note: $\mathrm{CO}_{2}$ emissions are measured on a production basis, meaning they do not correct for emissions embedded in traded goods.
OurWorldlnData.org/co2-and-other-greenhouse-gas-emissions/ $\cdot$ CC BY

Guide Questions for Reflection:

1. What is CO 2 and how does abundance of its emission affect us and the world?
2. What can you say about the trend of CO2 emissions by five countries?
3. What do you think are the factors that cause the difference in CO 2 for every country?
4. What other global pressing issues are likely associated with the rapid increase in CO2 emission?
5. There is a passage that says, "humanity needs more than Earth could offer." In relation to CO2, what could humanity do to save the earth from the harmful consequences of increasing CO2 emissions?

## LESSON PROPER

## APPLICATION (WHAT I CAN DO/ISAGAWA)

Each year, the average Filipino consumer adds 1.22 tons of carbon dioxide to the atmosphere (https://www.worldometers.info/co2-emissions/philippines-co2-emissions/). A total of 126922662 tons of carbon dioxide was produced by the country in 2016. It came mainly from our food, transportation, and homes. In addition, Philippine Statistics Office reports that our country's population at year 2016 was 103663816 and it is continually rising at an average rate of $1.27 \%$ per year according to the data from Philippine Statistics Authority.

Directions: Using the above information, fill in the table with computed values and answer the follow-up questions.

| Year | Population <br> (P) <br> Use 1.21\% <br> average increase of population | Average $\mathrm{CO}_{2}$ <br> footprint per <br> capita in (tons/capita) | Population X $\mathrm{CO}_{2}$ footprint per capita | Change |
| :---: | :---: | :---: | :---: | :---: |
| 2016 | 103663816 | Baseline | 126922662 | Baseline |
| 2017 | (1) | 1.22 <br> tons/capita | (2) | (3) |
| 2018 | (4) | $\begin{gathered} 1.22 \\ \text { tons/capita } \end{gathered}$ | (5) | (6) |
| 2019 | (7) | $1.22$ <br> tons/capita | (8) | (9) |

Questions to ponder:

1. What is the difference between the population in Year 2018 and Year 2017? How about in year 2019 and 2018?
2. Can we consider the progression of population in the Philippines as an arithmetic sequence? Why?
3. Using the given data, what do you think is the projected population of 2021?
4. What is the total CO2 emission produced by Philippines in 2021?
5. What do you think you could do as a Filipino and as a citizen of the world to reduce your CO2 contribution to the Earth's atmosphere

## ASSESSMENT

## TAYAHIN

You are now going to take your final assessment to see how much you have learned in this module.

## Part A

Directions: Choose the letter that corresponds to the correct answer.

1. Find the 10th term of the arithmetic sequence given that al $=4$ and $d=7$
a. 67
b. 28
c. 96
d. 85
2. If $a 7=3$ and $d=-3$, what is the 7 th term?
a. -9
b. -75
c. 35
d. 15
3. Solve the 20th term of the sequence $-2,6,14,22,30, \ldots$.
a. 158
b. 162
c. -100
d. 150
4. What should be the value of $x$ so that $x+2,3 x-2,7 x-12$ will form an arithmetic sequence?
a. 6
b. 4
c. 2
d. 3
5. Which among the given situations DOES NOT illustrate an arithmetic sequence?
a. In the Philippines, the number of cases can be modeled by the equation an $=1$ $000(1.61 n-1)$, where an is the number of COVID-19 infections after $n$ months.
b. There are many ways to increase carbon in soils. Planting cover crops when fields are otherwise bare can extend photosynthesis throughout the year, sequestering about half a metric ton of CO2 per acre per year.
c. Carbon-removal potential from forests and trees outside forests in the United States alone is more than half a gigaton per year
d. Between 2009-2018, the growth rate of CO2 emission has been 2.3 ppm per year.

## Part B. Performance Task

According to Tree Nation publication in January 2020, planting six trees per month is enough to compensate for the CO2 emissions we produce. Using this information, formulate a household CO2 reduction or offset plan that you would propose to your family in response to the call to save the earth from the hazardous effects of climate change. Use the attached template for your output and note that it will be graded using the following rubric.

## ASSESSMENT

## TAYAHIN

## Rubric for Rating

| Score | Descriptor |
| :---: | :--- |
| $\mathbf{4}$ | The written plan which includes computations involving arithmetic sequence are <br> completely accurate. Responses to the questions are very clear, highly relevant and <br> reflective. |
| $\mathbf{3}$ | The written plan includes computations involving arithmetic sequence are with 1 to <br> 2 mistakes. Responses to the questions are clear, relevant and reflective. |
| $\mathbf{2}$ | The written plan includes computations involving arithmetic sequence are with 3 to <br> 4 mistakes. Responses to the questions are with minimal inconsistencies, less <br> relevant and reflective. |
| $\mathbf{1}$ | The written plan includes computations involving arithmetic sequence are with more <br> than 4 mistakes. Responses to the questions are unclear, impossible to follow, <br> superficial and with so much inconsistencies. |
| $\mathbf{0}$ | Nowritten report was made. |

## Household $\mathrm{CO}_{2}$ Offset Plan

Family Name: $\qquad$
Number of household members: $\qquad$
Number of trees to be planted for the whole household per month: $\qquad$
Example: if there are three household members, then each month, the family is to plant $3 \times 6=18$ trees.
Directions: Fill in each cell of the table and provide response to the questions. You can ask help from other family members in accomplishing the plan.


## ANSWER KEY

## SUSI SA PAGWAWASTO

## Pretest (What I Need/Subukin)

Part A.

1. B
2. B
3. D
4. C

## Review (What's In/Balikan)

1. D 2. A

Activity (What's New/Tuklasin)

| Year | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| CO2 in ppm | 390 | 392 | 394 | 396 | 398 | 340 |

Answers for Guide Questions:

1. 392 ppm, 394 ppm. Simply by adding 2pmm from the previous year.
2. 340 ppm. 414 ppm.
3. 100 years from now, or 100 years from 2021 is 112 years from 2009, so 614ppm.
4. answers may vary

## Discussion (What Is It/Talakayin)

Answers to Guide Questions

1. answers may vary
2. answers may vary

## Generalization

1-4 Answer may vary

## Reflection (Why Is It Meaningful and Relevant/Isapuso)

Answer may vary.

## Application (What I Can Do/Isagawa)

1. 104918148
2. 128000140.8
3. 1077478.772
4. 106187658
5. 129548942.5
6. 1548801.703
7. 107472528
8. 131116484.7
9. 1567542.204

## Answers to Questions to Ponder

1. 1269509.59, 1284870.66
2. No, the differences are not equal.
3. 134308700.4
4. Answer may vary

## Assessment/Tayahin

## Part A

1. A
2. B
3. D
4. D
5.A

Part B -Answer may vary

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